

MATEMATICAS. BC2 TEMA 7: Límites

$$1 \lim_{x \rightarrow \infty} (\sqrt{x^2 + 3x} - \sqrt{x^2 + x}) \quad 2 \lim_{x \rightarrow \infty} \left(\frac{x^2}{x-1} - \frac{x^2 + 1}{x-2} \right) \quad 3 \lim_{x \rightarrow \infty} \frac{7x-1}{\sqrt[3]{5x^3 + 4x - 2}}$$

$$4 \lim_{x \rightarrow \infty} \frac{\sqrt{4x^4 + x^2 + 1}}{x^2 + 1} \quad 5 \lim_{x \rightarrow \infty} \frac{(x^2 + 1)^2 - 3x^2 + 3}{x^3 - 5} \quad 6 \lim_{x \rightarrow \infty} \frac{\log(x^8 - 5)}{x^2}$$

$$7 \lim_{x \rightarrow \infty} \frac{3^x - 1}{\sqrt{x^7 + x^5}} \quad 8 \lim_{x \rightarrow \infty} \frac{x^7 + x^5 + x^3}{\left(\frac{1}{2}\right)^x} \quad 9 \lim_{x \rightarrow 0} \frac{2}{3 + 4^{\frac{1}{x}}}$$

$$10 \lim_{x \rightarrow \infty} \left(\sqrt{18x^2 + 1} - \frac{1}{\sqrt{32x^2 - 3}} \right) \quad 11 \lim_{x \rightarrow 0} \frac{(1+x)^2 - 1}{x} \quad 12 \lim_{x \rightarrow 3} \frac{x^2 - 9}{x^2 - 5x + 6}$$

$$13 \lim_{x \rightarrow 3} \frac{\sqrt{x+1} - 2}{x-3} \quad 14 \lim_{x \rightarrow \infty} \left(1 + \frac{1}{x+2} \right)^{x-1} \quad 15 \lim_{x \rightarrow \infty} \left(1 - \frac{2}{3x} \right)^x$$

$$16 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n+1} \right)^{\frac{3n^2+2}{5n-3}} \quad 17 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n+1} \right)^{\frac{-3n^2+2}{5n-3}} \quad 18 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n+1} \right)^{\frac{-3n^2+2}{5n^2-3}}$$

$$19 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n^3+1} \right)^{\frac{3n^2+2}{5n-3}} \quad 20 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n^3+1} \right)^{\frac{-3n^2+2}{5n-3}} \quad 21 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n^2+1} \right)^{\frac{-3n+2}{5n^2-3}}$$

$$22 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n^2+1} \right)^{\frac{-3n^2+2}{5n-3}} \quad 23 \lim_{x \rightarrow \infty} \left(\frac{2n^2}{3n^2+1} \right)^{\frac{3n^2+2}{5n-3}}$$

SOLUCIONES:

1.
 $\lim_{x \rightarrow \pm\infty} (\sqrt{x^2+3x} - \sqrt{x^2+x}) \rightarrow 1$

2.
 $\lim_{x \rightarrow \pm\infty} \left(\frac{x^2}{x-1} - \frac{x^2+1}{x-2} \right) \rightarrow -1$

3.
 $\lim_{x \rightarrow \pm\infty} \left(\frac{7x-1}{\sqrt[3]{5x^9+4x-2}} \right) \rightarrow \frac{7 \cdot \sqrt[3]{5^8}}{5}$

4.
 $\lim_{x \rightarrow \pm\infty} \left(\frac{\sqrt{4x^4+x^2+1}}{x^2+1} \right) \rightarrow 2$

5.
 $\lim_{x \rightarrow \pm\infty} \left(\frac{(x^2+1)^2 - 3x^2 + 3}{x^3 - 5} \right) \rightarrow \pm\infty$

8.
 $\lim_{x \rightarrow \pm\infty} \frac{x^7 + x^5 + x^3}{\left(\frac{1}{2}\right)^x} \rightarrow +\infty$

9.
 $\lim_{x \rightarrow \pm\infty} \frac{2}{3+4\frac{1}{x}} \rightarrow 0.5 \quad \square$

10.
 $\lim_{x \rightarrow \pm\infty} \left(\sqrt{18x^2+1} \cdot \frac{1}{\sqrt{32x^2-3}} \right) \rightarrow \frac{3}{4}$

11.
 $\lim_{x \rightarrow 0} \frac{(1+x)^2 - 1}{x} \rightarrow 2$

12.
 $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x^2 - 5x + 6} \rightarrow 6$

17)

$$\lim_{x \rightarrow \pm\infty} \frac{2x^2}{3x+1} \frac{-3x^2+2}{5x-3} \rightarrow 0$$

18./ $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x+1} \right) \frac{-3x^2+2}{5x^2-3} \rightarrow 0$

19./ $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x^3+1} \right) \frac{3x^2+2}{5x-3} \rightarrow 0$

20./ $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x^3+1} \right) \frac{-3x^2+2}{5x-3} \rightarrow +\infty$

21./ $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x^2+1} \right) \frac{-3x+2}{5x^2-3} \rightarrow 1 \quad \square$

6.
 $\lim_{x \rightarrow \pm\infty} \frac{\log(x^8-5)}{x^2} \rightarrow 0$

7.
 $\lim_{x \rightarrow \pm\infty} \left(\frac{3^x - 1}{\sqrt{x^7 + x^5}} \right) \rightarrow +\infty$

13.
 $\lim_{x \rightarrow 3} \frac{\sqrt{x+1} - 2}{x-3} \rightarrow \frac{1}{4}$

14.
 $\lim_{x \rightarrow \pm\infty} \left(1 + \frac{1}{x+2} \right)^{x-1} \rightarrow e$

15.
 $\lim_{x \rightarrow \pm\infty} \left(1 - \frac{2}{3x} \right)^x \rightarrow \frac{\sqrt[3]{e}}{e}$

16.
 $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x+1} \right) \frac{3x^2+2}{5x-3} \rightarrow +\infty$

22./ $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x^2+1} \right) \frac{-3x^2+2}{5x-3} \rightarrow +\infty$

23./ $\lim_{x \rightarrow \pm\infty} \left(\frac{2x^2}{3x^2+1} \right) \frac{3x^2+2}{5x-3} \rightarrow 0$